

Performance of Transmission Lines.

The important considerations in design and operation of the transmission line are the determination of voltage drop, line losses and efficiency of transmission. These values are greatly influenced by the line constants (Resistance, inductance, capacitance) of the transmission line. For instance, the line drop depends upon the above three line constants. Similarly, the resistance of transmission lines conductors is the most important cause of power loss in the line and determines the transmission efficiency. In this module, I will develop formulas by which I can calculate voltage regulation, line losses and efficiency of transmission lines. These formulas are important for two principal reasons: firstly, they provide an opportunity to understand the effects of parameters of lines on bus voltages and the flow of power; secondly, they help in understanding of what is occurring in an electric power system.

Imp Classification of Overhead Transmission Lines.

Transmission line has 3 line constants R , L & C distributed uniformly along the whole length of the line. The resistance and inductance form series impedance. The capacitance existing between conductors for single phase line or from a conductor to neutral for a three phase line falls a shunt path throughout the length of the line. Therefore, capacitance effects introduced complications in transmission line calculation. Depending upon the manner in which capacitance is taken into account, the overhead transmission lines are divided as (1) short transmission lines, (2) medium transmission lines and (3) long transmission lines.

(1) Short Transmission Line.

When the length of an overhead transmission line is up to 50 km and the line voltage is comparatively low (< 20 kV), it is usually considered as short transmission line due to smaller length.

and lower voltage. The capacitance effect are lower and hence can be neglected they are while studying the performance of the short transmission line only resistance and inductance of the line are taken into account.

② Medium Transmission Line

When the length of an overhead transmission line is up to 50 to 150 km and the line voltage is moderately high ($100\text{ kV} < V < 100\text{ kV}$) it is considered as medium transmission line. Due to sufficient length & voltage of the line the capacitance effect is taken into account for purposes of calculations. The distributed capacitance of the line is lumped in the form of condensers shunted a/c the line at 1 or more points.

③ Long Transmission Lines

When the length of an overhead transmission line is more than 150 km and line voltage is very high ($> 100\text{ kV}$) it is considered as the long transmission line. For the treatment of such a line the line constants are considered uniformly distributed the whole length of line the rigorous methods are employed for solution of long transmission line.

Important terms

While studying the performance of transmission lines it is desirable to design its voltage regulation & transmission efficiency.

① Voltage regulation: When a transmission line is carrying current there is voltage drop in line due to resistance of line. The result is that receiving an voltage V_R of the line is generally less than sending an voltage V_S . This voltage drop ($V_S - V_R$) in the line is expressed as a percentage of receiving an voltage V_R is called voltage regulation.

The difference in voltage at the receiving end of a transmission line between the conditions of no load and full load is called voltage regulation, expressed as percentage of receiving end voltage. Mathematically, % voltage regulation is equal to $\frac{V_s - V_R}{V_R} \times 100$

Obviously it is desirable that the voltage regulation of line should be low i.e. increase in load ^{current} should make the difference in receiving end

② Transmission Efficiency: The power obtained at the receiving end of T line is generally less than sending end of line due to losses in line resistance. The ratio of receiving end power to sending end of power is of T line is called transmission efficiency of line.

$$\% \text{ Transmission efficiency } \eta_T = \frac{\text{receiving end power} \times 100}{\text{Sending end power}}$$
$$= \frac{V_R I_R \cos \phi_R}{V_s I_s \cos \phi_s} \times 100$$

Where V_R, I_R & $\cos \phi_R$ are the receiving end voltage & current & p.f.

while V_s, I_s & $\cos \phi_s$ are the corresponding values at the sending end.

15-02-17

Performance of single phase short transmission lines

A s. stated earlier the effects of line capacitance are neglected for short transmission line. Therefore, while studying performance of such a line only resistance and inductance of the line are taken in to account. The equivalent ckt of single phase short transmission line is shown in fig 3.1 Here the total line resistance and inductance are shown as concentrate or lumped instead of being distributed the ckt is simple A C series ckt

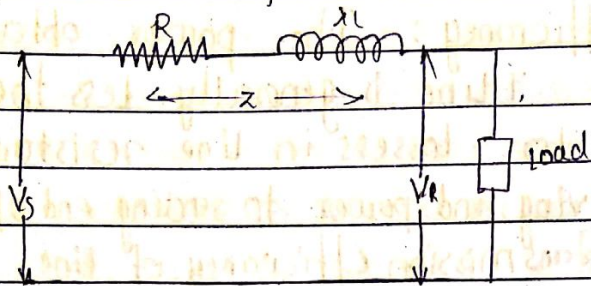


fig - 3.1

Let $I = \text{load c/n}$

$R =$ loop resistance i.e. resistance of both conductor

$X_L =$ loop reactance in Ohm

$V_R =$ Receiving end vty in V

$\cos \phi_R =$ Receiving end p.f (lag)

$V_S =$ sending end vty in V

$\cos \phi_S =$ sending end p.f (lag)

The phasor diagram of the line for lagging load p.f is as shown in fig 3.2

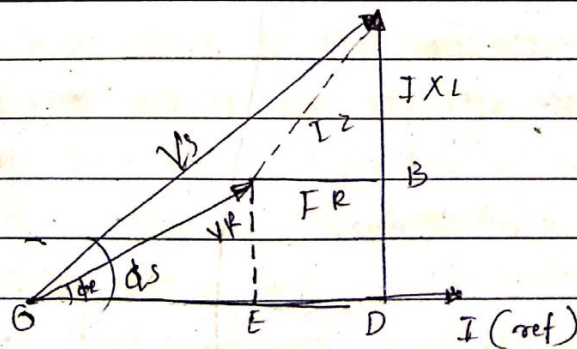


Fig (3.2)

From right angled ΔODC

$$OC^2 = OD^2 + DC^2$$

$$OC^2 = OD^2 + DC^2$$

$$V_S^2 = (OC + ED)^2 + (DB + BC)^2$$

$$V_S^2 = (V_R \cos \phi_R + I R)^2 + (V_R \sin \phi_R + j X_L)^2$$

$$V_S = \sqrt{(V_R \cos \phi_R + I R)^2 + (V_R \sin \phi_R + j X_L)^2} \quad \text{--- (3.1)}$$

$$\% \text{ Voltage regulation} = \frac{V_S - V_R}{V_R} \times 100 \quad \text{--- (3.2)}$$

$$\text{Sending end p.f. } \cos \phi_S = \frac{OD}{OC}$$

$$\cos \phi_S = \frac{V_R \cos \phi_R + I R}{V_S} \quad \text{--- 3.3}$$

$$\text{Power delivered } P_d = V_R I R \cos \phi_R \quad \text{--- (3.4)}$$

$$\text{Line losses} = P_L = I^2 R \quad \text{--- (3.5)}$$

$$\text{Power sent out} = P_S = V_R I R \cos \phi_R + I^2 R \quad \text{--- (3.6)}$$

$$\% \text{ transmission eff}^n = \frac{\text{Power delivered}}{\text{Power sent out}} \times 100$$

$$\% \eta = \frac{V_R I R \cos \phi_R}{V_R I R \cos \phi_R + I^2 R} \times 100 \quad \text{--- (3.7)}$$

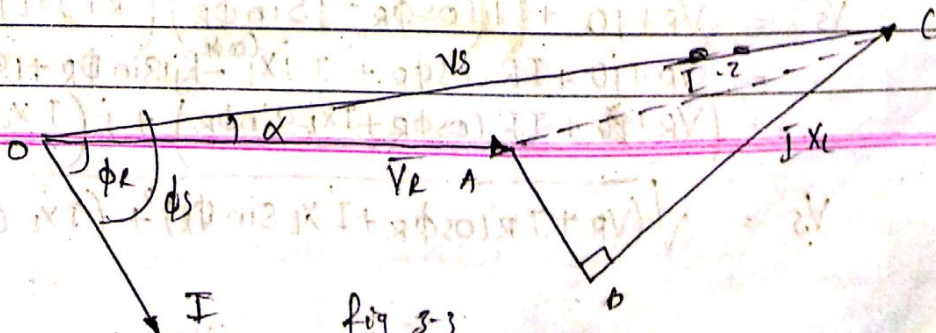
Key Point :-

Phasor diagram

Current I is taken as reference phasor. OA represents receiving end vtg V_R leading I by ϕ_R . AB represents the drop $I R$ (Resistive drop) in phase with I .

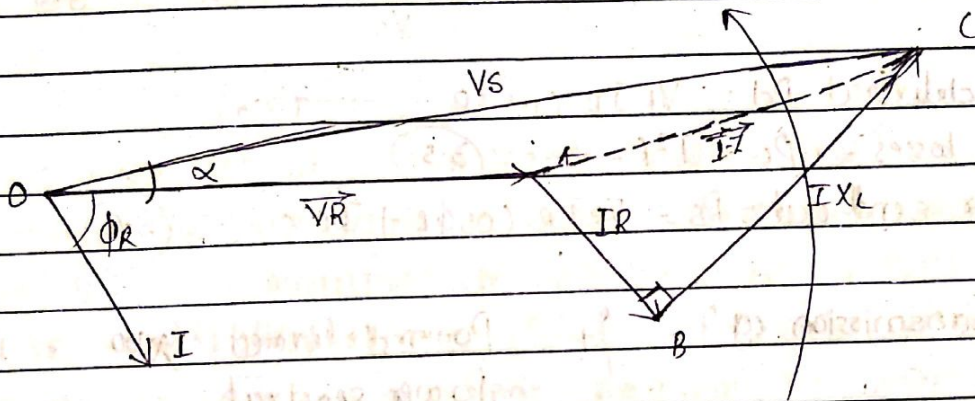
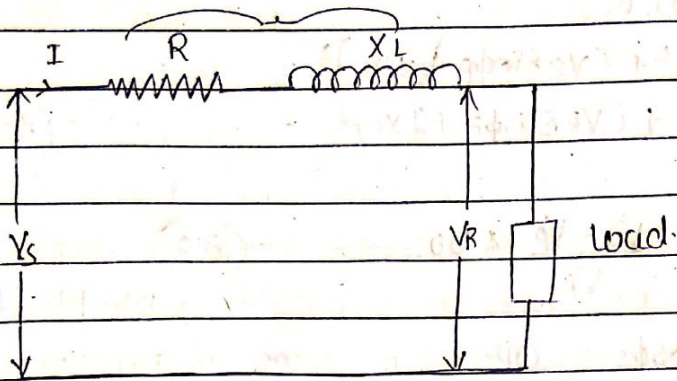
BC represents the inductive drop $j X_L$ and leads I by 90° . OC represents the sending end vtg V_S and lead current I by ϕ_S .

Keeping V_R as reference



Solution in Complex Notation.

It is of one convenient & Profitable to make line configuration in complex notation



Taking \$\vec{V}_R\$ as the reference phasor as shown in the fig-3.3 it is clear that \$\vec{V}_S\$ is the sum of \$\vec{V}_R\$ and ~~pro~~ \$\vec{I} \cdot \vec{Z}\$

$$\vec{V}_R = V_R + j0 \text{ (Reference)} \quad \text{--- (3.8)}$$

$$\vec{I} = I \angle -\phi_R \quad \text{--- (3.9)}$$

$$\vec{I} = I [\cos \phi_R - j \sin \phi_R] \quad \text{--- (3.10)}$$

$$\vec{Z} = R + jX_L \quad \text{--- (3.11)}$$

$$\therefore \vec{V}_S = \vec{V}_R + \vec{I} \cdot \vec{Z} \quad \text{--- (3.12)}$$

$$\vec{V}_S = V_R + j0 + I (\cos \phi_R - j \sin \phi_R) (R + jX_L) \quad \text{--- (3.13)}$$

$$= V_R + j0 + I R \cos \phi_R + I j X_L \cos \phi_R - R j I \sin \phi_R + I \sin \phi_R X_L$$

$$= (V_R + I R \cos \phi_R + I X_L \sin \phi_R) + j (I X_L \cos \phi_R - I R \sin \phi_R)$$

$$V_S = \sqrt{(V_R + I R \cos \phi_R + I X_L \sin \phi_R)^2 + (I X_L \cos \phi_R - I R \sin \phi_R)^2}$$

(3.14)

The second term under the square root eqⁿ (3.14) is quite small and can be neglected with reasonable accuracy.

∴ Approximate expression for V_s becomes

$$V_s = V_R + I R \cos \phi_R + I X_L \sin \phi_R \quad (3.15)$$

Key Points.

- 1) The approximate formula for V_s is eqⁿ no. (3.15) gives fairly correct results for lagging power factors however appreciable error is caused for leading power factor. therefore approximate expression for V_s should be used for lagging power factor only.
- 2) The solution in complex notation is in more present table for

Three phase short transmission lines.

20-02-14

For reasons associated with economics, transmission of electric power is done by 3 ϕ system. This system may be regarded as consisting of 3 ϕ circuits which wire transmitting $\frac{1}{3}$ rd of the total ^{power} ~~current~~ as a matter of convenience. We generally analyse 3 ϕ system by considering one phase only. therefore expression for regulation efficiency etc derived for a single phase line can also be applied to 3 ϕ system since only one phase is considered, phase ~~value~~ ^{value} of 3 ϕ system should be taken. thus V_s & V_R are the phase vtgs, where R & X_L are resistance and inductive reactance respectively.

fig-5 - eqⁿ ϕ ckt of 3.

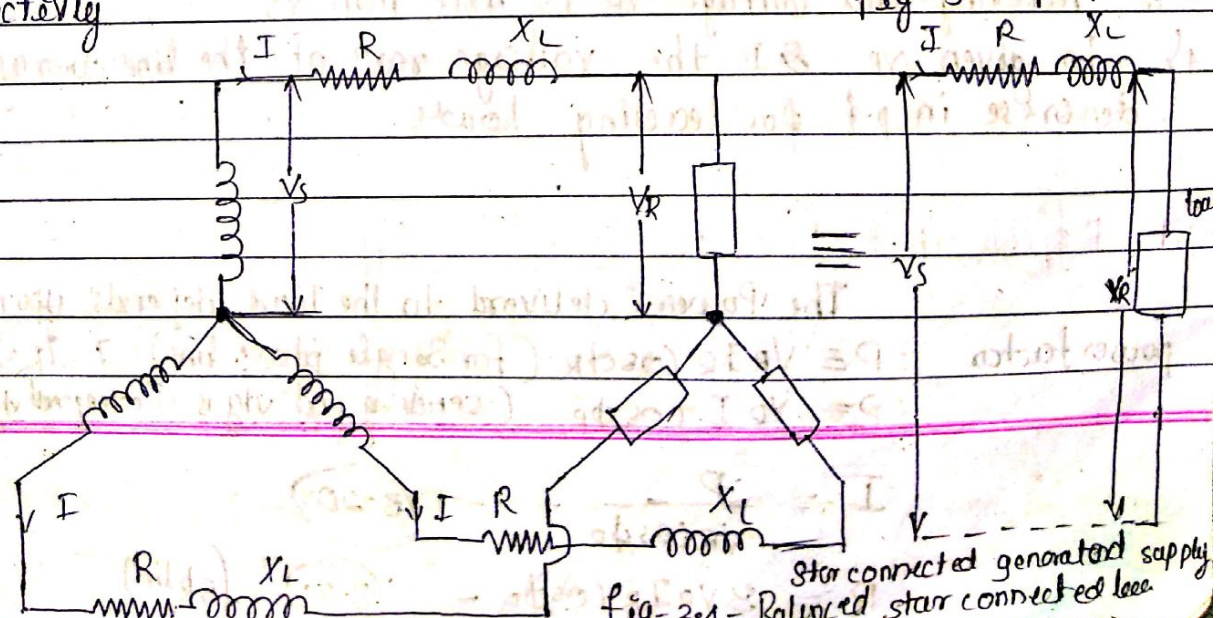


fig-3.4 - Balanced star connected gen. supply

Fig 3.4 shows a star connected generator supplying a balanced star connected load via transmission lines each conductor has resistance of $R \Omega$ and inductive reactance of $X_L \Omega$ fig 3.5 shows 1ϕ separately. The calculations can now be made in same way as for a single phase line.

* Effect of Load Powerfactor on regulation & Efficiency.

The regulation & eff of TL depends on considerable extent the p.f of the load

1) Effect on Regulation:

The expression for p.f of vty regⁿ of short TL is given by $\% \text{ Voltage regulation} = \frac{IR \cos \phi_R + IX_L \sin \phi_R}{V_R} \times 100$ (3.16)

(For lagging Powerfactor)

$\% \text{ Voltage regulation} = \frac{IR \cos \phi_R - IX_L \sin \phi_R}{V_R} \times 100$ (For Leading p.f) (3.17)

The following conclusions can be main by 3.16 & 3.17

1) When the p.f is lagging or unity or such leading that $IR \cos \phi_R > IX_L \sin \phi_R$ then voltage regulation is (+ve) that is receiving end voltage V_R will be less than

2) For a given V_R & I the vty regulation of line increases with decrease in p.f for lagging loads

3) When the load power factor is leading to this extent that $IR \cos \phi_R < IX_L \sin \phi_R$, then voltage regulation is negative i.e. receiving end voltage V_R is more than V_S

4) For given V_R & I the voltage regⁿ of the line decreases with decrease in p.f for leading loads

* Effect of P.F on Transmission Efficiency.

The Powers delivered to the load depends upon the powerfactor

$$P = V_R I_R \cos \phi_R \quad (\text{for single phase line}) \quad I = I_R = I_S \quad (3.18)$$

$$P = V_R I \cos \phi_e \quad (\text{sending end vty is = Receiving end vty}) \quad (3.19)$$

$$I = \frac{P}{V_R \cos \phi_R} \quad (3.20)$$

$$P = 3 V_R I_R \cos \phi_R \quad (3.21) \quad (3 \phi \text{ line})$$

$$P = 3 V_R I \cos \phi_R \quad (3.20)$$

$$\therefore I = \frac{P}{3 V_R \cos \phi_R}$$

$$I = \frac{P}{\sqrt{3} \times \frac{\sqrt{3} V_L}{\sqrt{3}} \cos \phi}$$

$$I = \frac{P}{\sqrt{3} \cdot V_L \cos \phi_R} \quad (3.24)$$

It is clear that in each case for a give amount of power to be transmitted (P) & receiving end voltage V_R the load current I is inversely proportional to $\cos \phi_R$ consequently, with the decrease in load power factor the load current and hence the line losses are increased. $\cos \phi_R \downarrow \Rightarrow I \uparrow \Rightarrow \text{loss} \uparrow$ this leads to the conclusion that transmission efficiency of the line decreases with decreasing load power factor & vice versa.

Example 3.1 A single phase overhead transmission line deliver 1100 kW at 33 kV at 0.8 power factor lagging. The total resistance and inductive reactance of the line are 10Ω and 15Ω resply. determine
 I) sending end voltage II) sending end power factor III) transmission efficiency

Given:

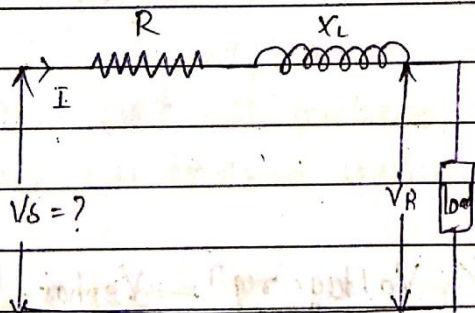
$$P = 1100 \text{ kW}$$

$$V_R (\text{phase}) = 33 \text{ kV}$$

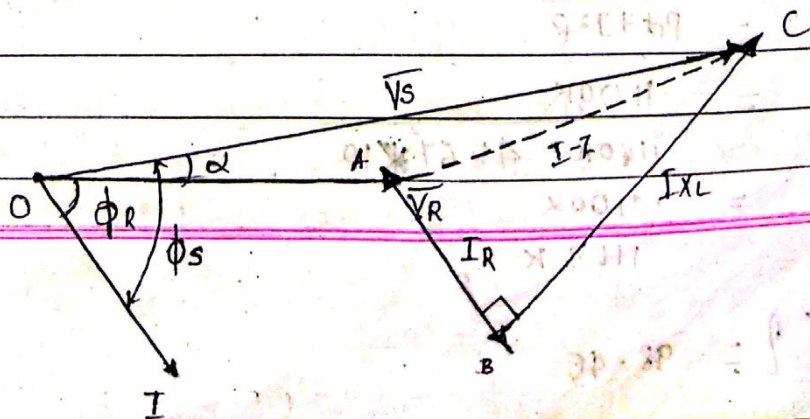
$$\cos \phi_R = 0.8 \text{ lag}$$

$$R = 10 \Omega$$

$$X_L = 15 \Omega$$



$$I = I_R + I_S$$



Solⁿ - Total line impedance $\vec{Z} = R + jX_L$

$$\vec{Z} = 10 + j15$$

$$\vec{V}_R = 33000V \Rightarrow 33k + j0 = \vec{V}_R$$

line current $I = \frac{P}{V_R \cos \phi_R}$
(load)

$$= \frac{1100k}{33k \times 0.8}$$

$$I = 41.67A$$

$$\vec{I} = I(\cos \phi_R - j \sin \phi_R)$$

$$= 41.67(0.8 - j0.6)$$

$$\vec{I} = 33.336 - j25.0023$$

$$\vec{V}_S = \vec{V}_R + \vec{I} \cdot \vec{Z}$$

$$= (33k + j0) + (33.336 - j25.0023) \times (10 + j15)$$

$$\vec{V}_S = 33709.39 + j250.02$$

$$V_S = \sqrt{(\text{Real } V_S)^2 + (\text{Imag } V_S)^2}$$

$$= \sqrt{(33709.39)^2 + (250.02)^2}$$

$$= 33708.4V$$

$$= 33.70KV$$

28-02-2017

$$\alpha = \tan^{-1} \left(\frac{\text{Imag } V_S}{\text{Real } V_S} \right)$$

$$= \tan^{-1} \left(\frac{250.02}{33709.39} \right)$$

$$\cos \phi_S = \cos(\phi_R + \alpha)$$

$$= \cos(36.86 + 0.425)$$

$$= 0.795 \text{ lag}$$

$$\alpha = 0.425^\circ$$

$$\% \eta = \frac{P_d}{P_s}$$

$$= \frac{P_d}{P_d + P_t}$$

$$= \frac{P_d}{P_d + I^2 R}$$

$$= \frac{1100k}{1100k + 41.67^2 \times 10}$$

$$= \frac{1100k}{1117k}$$

$$= 98.45\%$$

$$\% \text{ Voltage reg} = \frac{V_{s \text{phas}} - V_{r \text{phas}}}{V_{r \text{phas}}}$$

$$= 2.144\%$$

$$\% \eta = 98.45$$

Alternate

$$V_s = V_R + I \cdot R \cos \phi_R + I \cdot X_L \sin \phi_R$$

$$= 33708 \text{ V}$$

$$\cos \phi_s = \frac{V_R \cos \phi_R + I R}{V_s} \quad \text{\% Voltage reg.}$$

$$= 33\%$$

Ex 2

(2) An Overhead 3- ϕ transmission line delivers 5000 kW at 22 kV at 0.8 p.f lagging. The resistance and reactance of each conductor is 4Ω and 6Ω respectively. Determine i) V_s ii) % Voltage reg. iii) % transmission η . (iv) Sending end p.f

$$P_d = 5000 \text{ kW}$$

$$V_{R \text{ line}} = 22 \text{ kV}$$

$$V_{R \text{ phase}} = \frac{V_{R \text{ line}}}{\sqrt{3}} = 12.70 \text{ kV}$$

$$\cos \phi_R = 0.8 \text{ lag.}$$

$$R = 4 \Omega$$

$$Z = R + jX_L = (4 + j6) \Omega$$

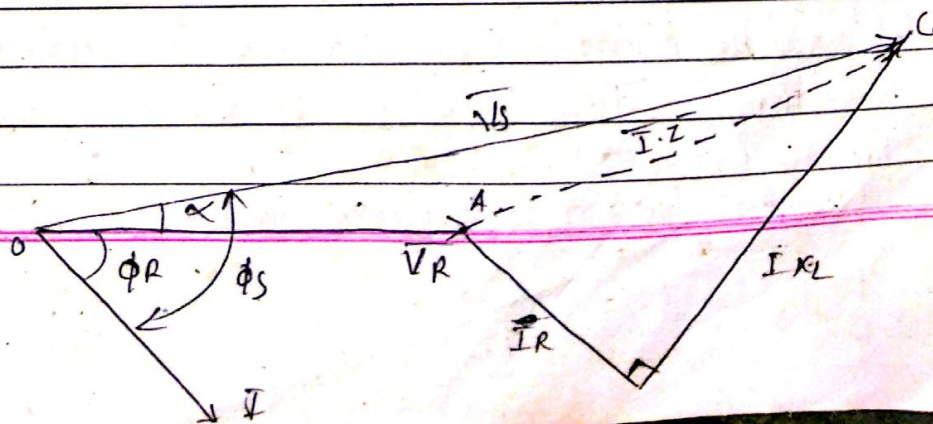
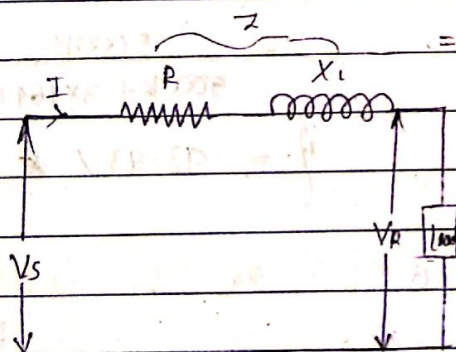
$$X_L = 6 \Omega$$

$$I = \frac{P_d}{3 V_R \cos \phi_R}$$

$$\overline{V_{R \text{ phase}}} = (12.70 + j0) \text{ V}$$

$$= \frac{5000 \text{ kW}}{3 \times 12.70 \text{ kV} \times 0.8}$$

$$= 164.09 \text{ A}$$



$$i) \vec{V}_s = \vec{V}_R + [I \cos\phi_R - j \sin\phi_R] \cdot [R + jX_L]$$

$$= 12.70k + j0$$

$$= (12.70k + j0) + [164.04(0.8 - j0.6)(4 + j6)]$$

$$\vec{V}_s = 13815.2 + 393.6j$$

$$V_{s, \text{phase}} = 13820.800 \quad \alpha = 1.632$$

$$V_{s, \text{line}} = \sqrt{3} \times 13820.800 \times 23.95$$

$$ii) \text{Voltage regulation} = \frac{V_R}{V_{s, \text{phase}}} \cdot V_{s, \text{phase}} - V_{R, \text{phase}} \times 100$$

$$= \frac{13820.80 - 12.70k \times 100}{12.70k}$$

$$= 8.82\%$$

$$iv) \text{Sending end p.f.} = \cos\phi_s = \cos(\phi_R + \alpha)$$

$$= \cos(36.86 + 1.632)$$

$$= 0.783$$

$$iii) \text{Percentage of transmission efficiency} = \frac{P_d}{P_s}$$

$$P_d = 93.93 \times P_s$$

$$= 93.93 \times (5000k + 3 \times 164.04^2 \times 4)$$

$$P_d = 5000k$$

$$= \frac{P_d}{P_d + P_l}$$

$$= \frac{P_d}{P_d + 3I^2R}$$

$$= \frac{5000k}{5000k + 3 \times 164.04^2 \times 4}$$

$$= 93.93\%$$

$$\eta = 93.93\%$$

HW

Q.3

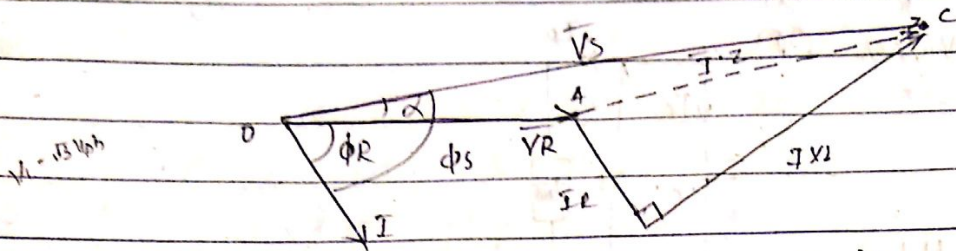
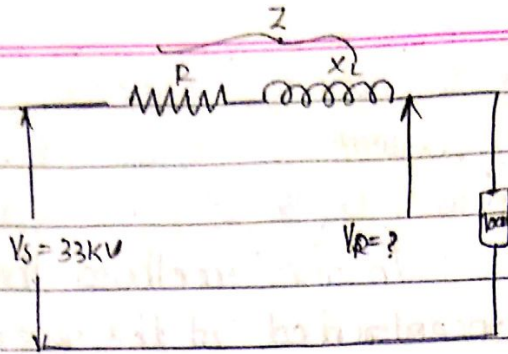
A 3 ϕ line delivers 3500kW at 0.8 p.f lag to a load if the sending end voltage is 33kV determine 1) the receiving end voltage 2) line current 3) transmission efficiency.

The resistance and reactance of each conductor is 5.31 Ω & 25.54 Ω respectively. (Refer "principles of power system" by VK mehta Pg. 236, Ex-10.5)

ex 10.6

pg-237 of VK Mehta and 10.7

$P_d = 3600 \text{ kW}$
 $\cos \phi_R = 0.8 \text{ lag}$
 $V_s = 33 \text{ kV}$
 $R = 5.31 \Omega$
 $X_L = 5.54 \Omega$



$V_{s \text{ line}} = 33 \text{ kV}$

$Z = R + jX_L$

$V_{\text{phase}} = \frac{33 \text{ kV}}{\sqrt{3}} = 19.052 \text{ kV}$

$Z = (5.31 + j5.54) \Omega$

$I = \frac{P_d}{3 V_{\text{phase}} \cos \phi_R} = \frac{3600 \text{ kW}}{3 \times 19.052 \text{ kV} \times 0.8} = 78.73 \text{ A}$
 $I = 62.985 + j47.238$

$\vec{V}_s = (V_R + j0) + I Z$
 $= 19.052 \text{ kV} + (62.985 + j47.238) (5.31 + j5.54)$

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* Medium Transmission Line.

1) End Condensers Method

In this method the capacitance of line is lumped or concentrated at the receiving end as shown in the fig-6

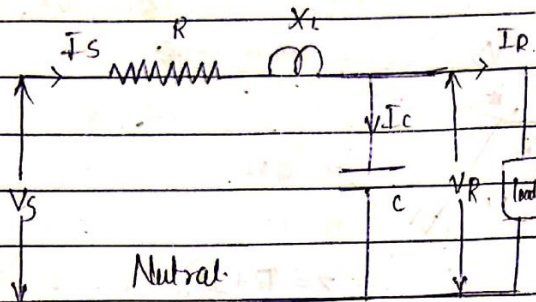


fig-3.6

This method of localising the line capacitance at the load end over estimates the effect of capacitance. fig-3.6 is one phase of the 2- ϕ transmission line which is shown as it is more convenient to work in phase instead of line to line values

Let $I_R =$ load current per phase.

$R =$ Resistance per phase.

$V_R =$ Receiving end vltg

$X_L =$ Inductive reactance per phase.

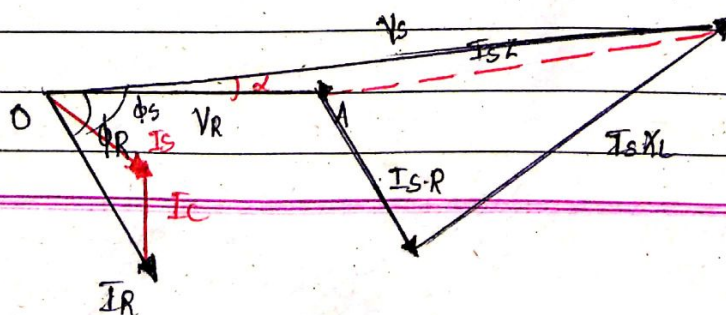
$C =$ Capacitance per phase.

$\cos\phi_R =$ Receiving end p.f (lag)

$V_s =$ Sending end voltage per phase.

$I_s =$ Sending end current per phase

The phasor diagram of circuit diagram 3.6 is shown in fig 3.7 taking V_R as reference phasor



$$I_s = I_R + I_C$$

$$\vec{V}_R = V_R + j0 \quad \text{--- (3.25)}$$

$$\text{load current or line current} = \vec{I}_R = I_R (\cos\phi_R - j\sin\phi_R) \quad \text{--- (3.26)}$$

$$\text{Capacitive current} = \vec{I}_C = \frac{\vec{V}_R}{X_C} = \frac{V_R}{1/j\omega C} = -j\omega C V_R$$

$$\text{Susceptance } (Y) \cdot |Y = G + jB \quad \vec{I}_C = jY \vec{V}_R \therefore \vec{I}_C = j2\pi f C \vec{V}_R \quad \text{--- (3.27)}$$

Sending end current I_S is the sum of load current I_R & capacitive current I_C .

$$\therefore \vec{I}_S = \vec{I}_R + \vec{I}_C \quad \text{--- (3.28)}$$

Substituting the value of I_R & I_C .

$$\vec{I}_S = I_R (\cos\phi_R - j\sin\phi_R) + j2\pi f C \vec{V}_R$$

$$\vec{I}_S = I_R \cos\phi_R + j(-I_R \sin\phi_R + 2\pi f C \vec{V}_R) \quad \text{--- (3.29)}$$

$$\text{Voltage drop per phase} = \vec{I}_S \vec{Z} \quad \text{--- (3.30)}$$

$$= I_R \cos\phi_R + j(2\pi f C V_R - I_R \sin\phi_R) (R + jX_L) \quad \text{--- (3.31)}$$

$$\text{Sending end voltage / phase} = \vec{V}_S = \vec{V}_R + \vec{I}_S \vec{Z}$$

$$\vec{V}_S = \vec{V}_R + \vec{I}_S (R + jX_L) \quad \text{--- (3.32)}$$

Thus, the magnitude of sending end voltage V_S can be calculated.

$$\% \text{ Voltage regulation} = \frac{V_S - V_R}{V_R} \times 100 \% \quad \text{--- (3.33)}$$

$$\% \text{ Transmission efficiency} = \frac{\text{Power delivered / phase}}{\text{Power delivered / phase} + \text{losses / phase}} \times 100 \quad \text{--- (3.34)}$$

Example

3.3 A medium single phase transmission line has the following constants:

$$\text{Resistance per km} = 0.25 \Omega$$

$$\text{Reactance per km} = 0.8 \Omega$$

$$\text{Susceptance per km} = 14 \times 10^{-6} \text{ S}$$

$$\text{Receiving end line voltage} = 66000 \text{ V}$$

Assuming the total capacitance of line localized at the receiving end a load, Determine 1) Sending end vty 2) sending end current 3) regulation 4) supply power factor, The line is delivering 15000 kW at 0.8 lagging p.f, draw the phasor diagram to illustrate your calculation.

Given

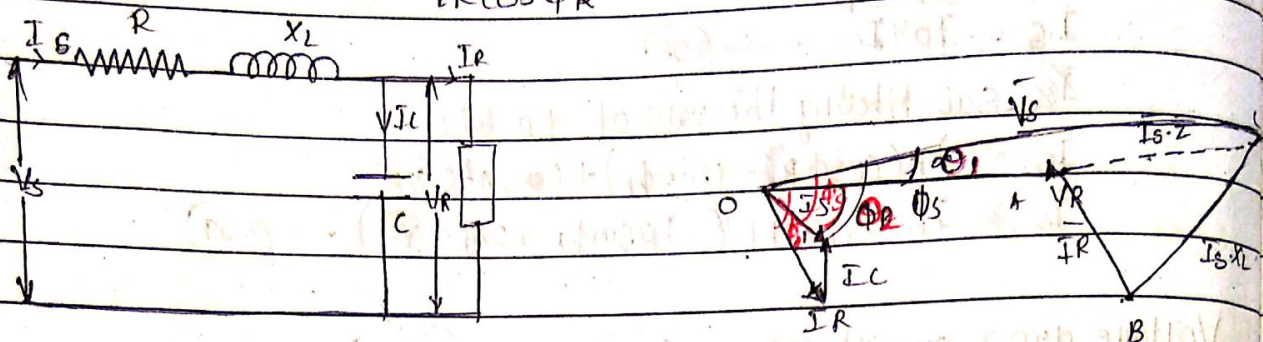
$$\text{Total resistance} = R = 0.25 \times 100 = 25 \Omega$$

$$\text{Total reactance} = X_L = 0.8 \times 100 = 80 \Omega$$

$$\text{Susceptance} = B = 14 \times 10^{-6} \times 100 = 1.4 \times 10^{-3} \text{ S}$$

$$V_R = 66 \text{ kV} \quad P = 15000 \text{ kW} \quad \cos \phi_R = 0.8 \text{ (lag)}$$

$$\text{load current } I_R = \frac{P}{V_R \cos \phi_R} = \frac{15000 \text{ kW}}{66 \text{ kV} \times 0.8} = 284 \text{ A}$$



$$\bar{V}_R = V_R + j0$$

$$= 66000 + j0$$

$$\bar{V}_R = 66000$$

$$\bar{I}_R = I_R (\cos \phi_R - j \sin \phi_R)$$

$$= 284 (0.8 - j0.6)$$

$$\bar{I}_R = 227.2 - j170.4$$

$$Y \bar{V}_C = G + jB$$

$$= 0 + j14 \times 10^{-3}$$

$$Y = 1.4 \times 10^{-3} \text{ S}$$

$$\bar{I}_C = jY \bar{V}_R$$

$$= j1.4 \times 10^{-3} \times 66000$$

$$= j92.4$$

$$Z = R + jX_L$$

$$Z = (25 + j80) \Omega$$

$$\bar{V}_S = \bar{V}_R + \bar{I}_S \bar{Z}$$

$$= (\bar{V}_R) + (\bar{I}_R + \bar{I}_C) \cdot (R + jX_L)$$

$$= (66 \text{ kV} + j0) + [(227.2 - j170.4) + j92.4] \cdot (25 + j80)$$

$$\bar{V}_S = 77920 + j16226$$

$$V_S = 79593 \angle 11.75^\circ$$

$$\theta_1 = \tan^{-1} \left(\frac{\text{Imag } V_S}{\text{Real } V_S} \right)$$

$$\theta_1 = \tan^{-1} \left(\frac{16226}{77920} \right)$$

$$= 11.75^\circ$$

$$\bar{I}_S = \bar{I}_R + \bar{I}_C$$

$$= 227.2 - j170.4 + j92.4$$

$$\bar{I}_S = 227.2 - j78$$

$$I_S = 240.21 \angle -18.95^\circ$$

$$\theta_2 = \tan^{-1} \left(\frac{\text{Imag } I_S}{\text{Real } I_S} \right)$$

$$= \tan^{-1} \left(\frac{-78}{227.2} \right)$$

$$\theta_2 = -17.99^\circ$$

$$\phi_s = \theta_1 + \theta_2$$

$$= 11.75 - 18.95$$

$$= -7.2$$

$$\%R = \frac{V_s - V_R}{V_R} \times 100$$

$$= \frac{79593 - 66k}{66k} \times 100$$

$$\cos \phi_s = \cos(-7.2)$$

$$\cos \phi_s = 0.992$$

$$\%R = 20.59\%$$

$$\% \eta_T = \frac{P_d}{P_d + I_s^2 R} \times 100$$

$$= \frac{15000k}{15000k + (240 \cdot 216)^2 \cdot 95} \times 100$$

$$\% \eta_T = 91.23\%$$

6/3/17

May 16
June 14

Nominal 'T' method

In this method the whole capacitance is assumed to be concentrated at the mid point of the line and half the line resistance and half the line reactance are lumped on either side as shown in the fig 3-8

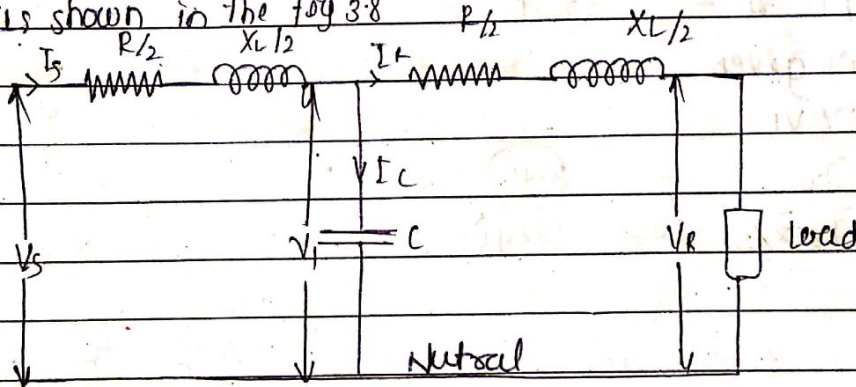


fig. 3-8

In this arrangement the full charging current flows over half of the T.L in fig 3-8 above fig shows 1 ϕ of a 3 ϕ T.L as it is advantage to work on 1 ϕ instead of line to line values let

V_s = Sending end voltage / phase.

R = resistance / phase.

I_r = Load current per phase

X_L = Inductive reactance per phase.

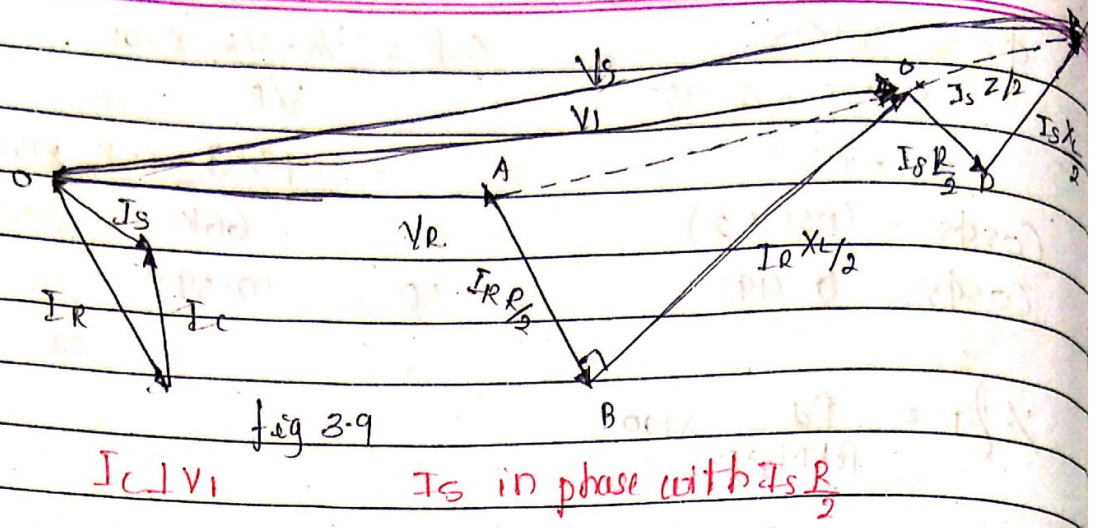
C = Capacitance per phase

$\cos \phi_R$ = Receiving end p.f

V_R = Receiving end vly. per phase

V_1 = Voltage a/c capacitor C.

$\cos \phi_s$ = Sending end p.f



$$\bar{V}_R = V_R + j0 \quad \text{--- (3-35)}$$

$$\bar{I}_R = I_R (\cos\phi_R - j\sin\phi_R) \quad \text{--- (3-36)}$$

voltage a/c capacitor.

$$\bar{V}_i = \bar{V}_R + \bar{I}_R \bar{Z}/2 \quad \text{--- (3-37)}$$

$$\bar{V}_i = (V_R + j0) + I_R (\cos\phi_R - j\sin\phi_R) \cdot \left(\frac{R}{2} + j \frac{X_L}{2} \right) \quad \text{--- (3-38)}$$

$$\bar{I}_c = \frac{\bar{V}_i}{X_c} = \frac{V_i}{\frac{1}{j\omega C}} = j\omega C V_i$$

$$I_c = j\omega C \cdot \bar{V}_i \quad \text{--- (3-39)}$$

If γ or B is given

$$I_c = j\gamma \bar{V}_i$$

$$\bar{I}_s = \bar{I}_R + \bar{I}_c \quad \text{--- (3-40)}$$

$$\bar{V}_s = \bar{V}_i + \bar{I}_s \bar{Z}/2 \quad \text{--- (3-41)}$$

(3-4) A 2 ϕ 50Hz overhead T.L 100km long has the following constant resistance / km/phase = 0.1 $\frac{\Omega}{km}$
 Capacitive susceptance / km/phase = 6.04 $\times 10^{-4}$ seimens
 Determine 1) I_s 2) V_s 3) $\cos\phi_s$ 4) η_T
 when supplying a balanced load of 10000 kW at 66 kV at 0.8 p.f (lag) use nominal T method

$$R = 0.1 \times 100 = 10 \Omega$$

$$X_L = 0.9 \times 100 = 20 \Omega$$

$$B = 0.04 \times 10^{-4} \times 100 = 4 \times 10^{-4} \text{ S} \quad I_R = 109A$$

$$P_d = 10000 \text{ kW}$$

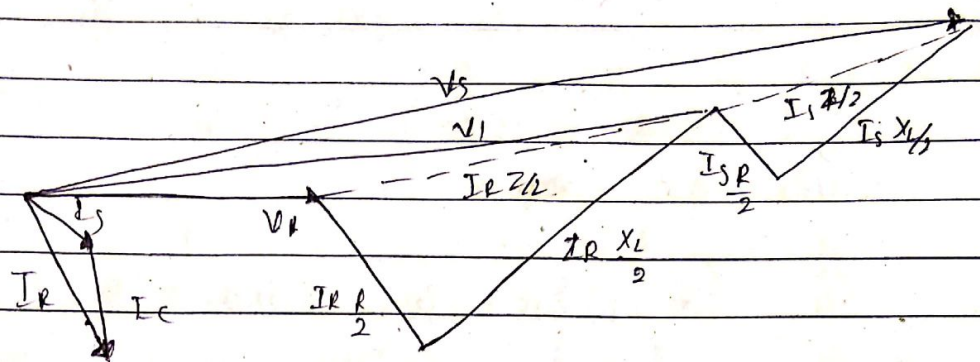
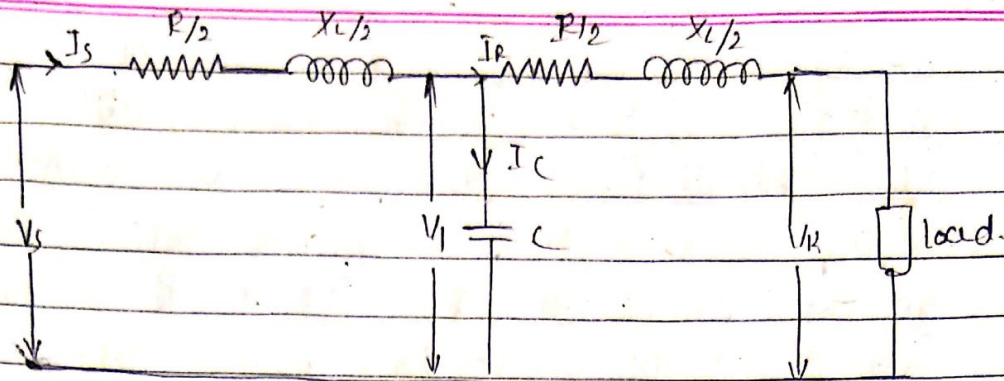
$$V_{RL} = 66 \text{ kV}$$

$$Z = R + jX_L$$

$$Z = (10 + j20) \Omega$$

$$\therefore V_{Rph} = 38.105 \text{ kV}$$

$$\bar{V}_R = 38.105 + j0$$



I will solve the above problem as earlier as possible and I know how to solve the problem. and I will be definitely solve it & I will very happy after solving the problem

$$I_R = \frac{P_d}{V_R \cos \phi_R}$$

$$\bar{I}_R = I_R (\cos \phi_R - j \sin \phi_R)$$

$$= 0.328 (0.8 - j0.6)$$

$$I_R = \frac{10000}{38.105 \text{ kV} \times 0.8}$$

$$\bar{I}_R = 0.2624 - j0.1968$$

$$I_R = 0.328$$

$$\bar{V}_1 = \bar{V}_R + \bar{I}_R \bar{Z}/2$$

$$\bar{I}_c = jY\bar{V}_1$$

$$= 38.105 + [(0.2624 - j0.1968)(5 + j10)]$$

$$\bar{I}_c = \{ 4 \times 10^4 \times 4.1385 + 1.64j \} \quad \bar{V}_1 = 41.385 + 1.64j$$

=

Jan 19
T-1002

3.5

HW

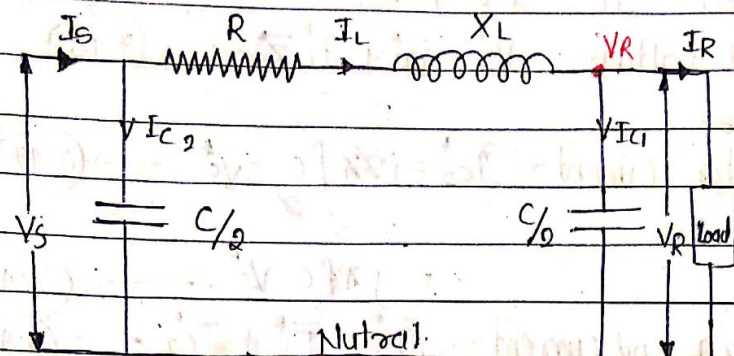
10.12.19 295

I will solve the above problem as follows and I know
how to solve the question and I will be able to solve it if I
keep solving after solving the question.

$$\begin{aligned} I_1 &= \int_{-\infty}^{\infty} f(x) \delta(x-a) dx \\ &= f(a) \end{aligned}$$
$$\begin{aligned} I_2 &= \int_{-\infty}^{\infty} f(x) \delta(x-a) dx \\ &= f(a) \end{aligned}$$
$$\begin{aligned} I_3 &= \int_{-\infty}^{\infty} f(x) \delta(x-a) dx \\ &= f(a) \end{aligned}$$

Nominal 'T' Method

In this method capacitance of each conductor (i.e. line to neutral) is divided into halves; one half is being lumped at the sending end and the other half at the receiving end as shown in the fig-3.10. It is obvious that capacitance at the sending end has less effect on the line drop however its charging end must be added to obtain the total sending end current.



Taking the V_R as 0 reference. Fig 3-10

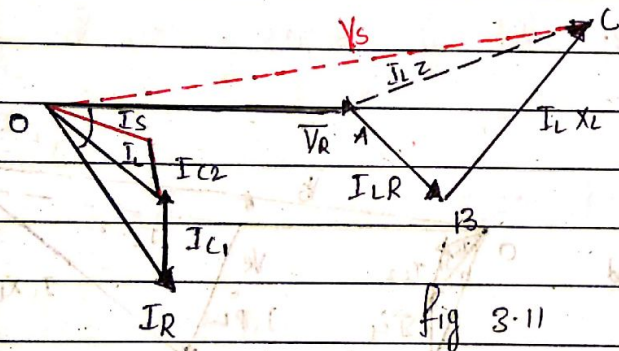


Fig 3-11

Let I_R = load current per phase,

R = resistance per phase ; X_L = reactance per phase

V_R = receiving end voltage per phase,

C = capacitor per phase

$\cos \phi_R$ = receiving end power factor

V_S = sending end voltage per phase.

I_S = Sending end current per phase.

The phasor diagram is as shown in fig 2.11 taken receiving end voltage as reference v_r.

$$\vec{V}_R = V_R + j0 \quad \text{--- (3.42)}$$

$$\text{Load current } \vec{I}_R = I_R (\cos\phi_R - j\sin\phi_R) \quad \text{--- (3.43)}$$

$$\text{charging c/m of capacitor at receiving end } \vec{I}_{C1} = j2\pi f C \vec{V}_R \quad \text{--- (3.44)}$$

$$I_{C1} = jY \vec{V}_R$$

$$\text{Line current } \vec{I}_L = \vec{I}_R + \vec{I}_{C1} \quad \text{--- (3.45)}$$

$$\text{Sending end voltage} = \vec{V}_S = \vec{V}_R + \vec{I}_L \vec{Z} \quad \text{--- (3.46)}$$

~~3.6~~

~~A 3φ 50Hz~~

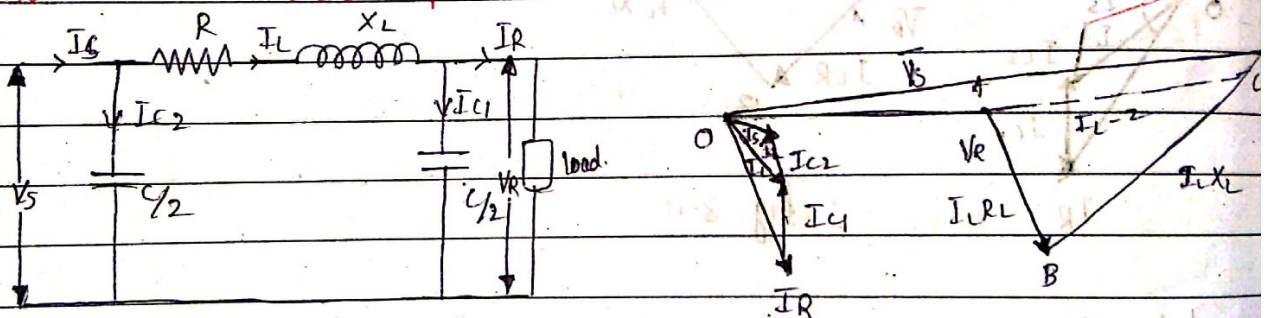
$$\text{2nd capacitor current} = \vec{I}_{C2} = j2\pi f C \vec{V}_S \quad \text{--- (3.47)}$$

$$= j\pi f C \vec{V}_S \quad \text{--- (3.48)}$$

$$\text{Sending end current} = \vec{I}_S = \vec{I}_L + \vec{I}_{C2} \quad \text{--- (3.49)}$$

10/3/17

(3-6) A 3φ 50Hz, 150km line has resistance, inductive reactance, capacitive admittance are 0.1Ω, 0.5Ω & 3x10⁻⁶ sem/km/line respectively. If the line delivers 50MW at 110kV and 0.8 PF (lag) determine the sending end v_t & current assume nominal π circuit for line.



$$\text{Sending end voltage} = \vec{V}_S = \vec{V}_R + \vec{I}_L \vec{Z}$$

$$V_R = 110k$$

$$\vec{V}_R = 110k - 63.568k + j0 \text{ V}$$

$$\vec{I}_R = \frac{P}{\sqrt{3} V_R \cos\phi_R} \quad \text{or} \quad \frac{P}{3 V_R \text{ phase } \cos\phi_R} = I_R (\cos\phi_R - j\sin\phi_R)$$

$$= \frac{50M}{\sqrt{3} 110k \times 0.8}$$

$$= \frac{50M}{3 \times 63.568 \times 0.8}$$

$$I_R = 328.03 \text{ A}$$

$$\begin{aligned}\vec{I}_L &= I_L (\cos\phi_R - j\sin\phi_R) \\ &= 328.03 (0.8 - j0.6) \\ &= 262.424 - j196.81\end{aligned}$$

$$\begin{aligned}I_R &= P \\ &= \frac{3 \times V_{Rphas} \cos\phi_R}{3 \times 63.508 \text{ k} \times 0.8} \\ &= 328.042\end{aligned}$$

$$\begin{aligned}I_{C1} &= j \frac{Y}{2} \cdot V_{Rpb} \\ &= j \frac{3 \times 10^{-6} \times 150 \times 63.508 \text{ k}}{2}\end{aligned}$$

$$\vec{I}_{C1} = j14.30 \text{ A}$$

$$\begin{aligned}\vec{I}_R &= I_R (\cos\phi_R - j\sin\phi_R) \\ &= 328.042 (0.8 - j0.6) \\ &= 262.43 - j196.825\end{aligned}$$

$$\vec{Z}_c = 15 + j75 \Omega$$

$$\begin{aligned}\vec{I}_L &= \vec{I}_R + \vec{I}_{C1} \\ &= 262.43 - j196.825 + j14.30 \\ &= 262.43 - j182.525 \text{ A}\end{aligned}$$

$$\begin{aligned}\vec{V}_S &= \vec{V}_{Rphas} + \vec{I}_L \vec{Z}_c \\ &= 63.508 \text{ k} + (262.43 - j182.525) (15 + j75)\end{aligned}$$

$$\vec{V}_S = 81.133 \text{ k} + 16.94 \text{ k}$$

$$\vec{V}_S = 82884.3 \angle 11.79^\circ$$

$$V_S = 82.884 \text{ kV}$$

$$\begin{aligned}\vec{I}_{C2} &= j \frac{Y}{2} \vec{V}_S \\ &= j \frac{4.5 \times 10^{-9}}{2} \cdot (81126 + j16941)\end{aligned}$$

$$\vec{I}_{C2} = -3.81 + j18.25 \text{ A}$$

$$\vec{I}_S = \vec{I}_L + \vec{I}_{C2}$$

$$= 262.43 - j182.525 + (-3.81 + j18.25)$$

$$\vec{I}_S = 258.62 - j164.275$$

$$I_S = 306.38$$

HW

Pg - 248

Ex - 10-14

[Faint, mostly illegible handwritten notes and equations are visible throughout the page, appearing as bleed-through from the reverse side. Some fragments of text and mathematical symbols are discernible.]

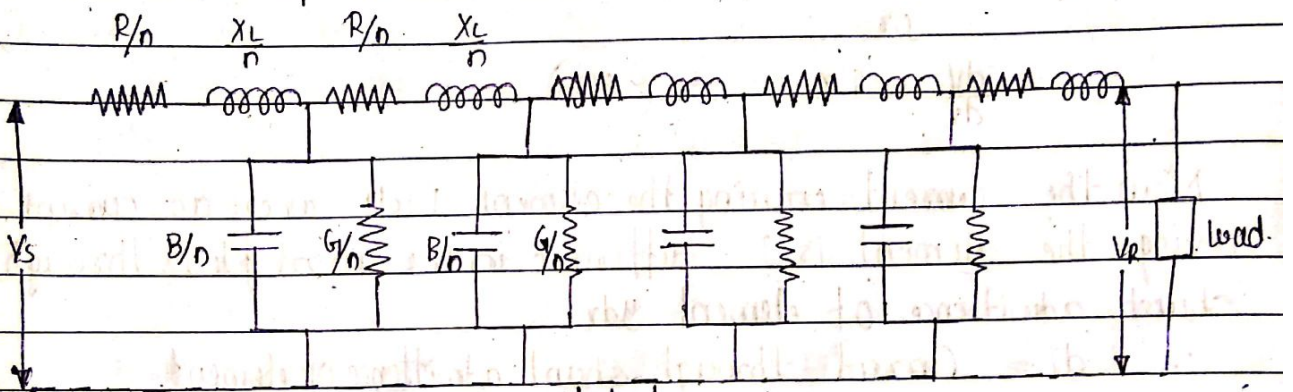
11/3/17

Long Transmission Lines

Method - Careful attention
 rigorous - with calculation

It is well known to me that line constants of transmission line are uniformly distributed over the entire length of line however, reasonable accuracy can be obtained in line calculation for short and medium transmission line by considering these constants are lumped

If such an assumption of lumped constant is applied to long TL (having length excess of about 150 km), it is found that ~~series~~ serious errors are introduced in performance calculation. Therefore in order to obtain the fair degree of accuracy in performance calculations in long transmission line. The line constants are uniformly distributed throughout the length, rigorous mathematical treatment is required for the solution of long transmission lines.



Neutral Fig - 3.12

Fig 3.12 shows the equivalent circuit of a 3 ϕ long transmission line on a phase to neutral bases. The whole length of line is divided into 'n' sections each section having line constants $\frac{1}{n}$ th of those for the line.

Analysis of long transmission line (Rigorous Method)

Fig 3.13 below shows 1 ϕ and neutral connection of a 3 ϕ line with impedance and shunt admittance of line is uniformly distributed.

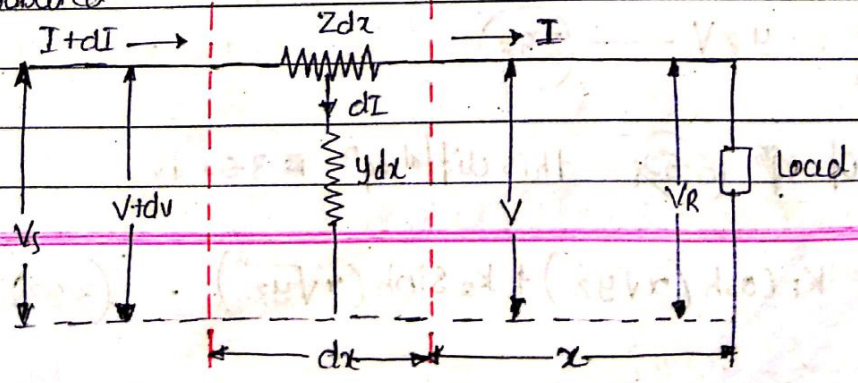


Fig (3.13)

Consider a small element in the line of length 'dx' situated at x from the receiving end.

Let $z =$ Series impedance of the line per unit length

$y =$ Shunt Admittance of the line per unit length

$V =$ Voltage at end of element toward receiving end.

$V+dv =$ Voltage at the end of element toward sending end.

$I+dI =$ Current entering the element dx .

$I =$ Current leaving the element dx .

then for the small element dx ,

$z dx =$ series impedance of element dx

$y dx =$ shunt admittance

Obviously, $dv = I z dx$.

or

$$\frac{dv}{dx} = I z \quad \text{--- (3.50)}$$

Now the current entering the element $I+dI$ where as current leaving the element is I difference in the current flows through shunt admittance of element $y dx$.

$\therefore dI =$ Current through shunt admittance of element

$$dI = y dx$$

$$\text{then } \frac{dI}{dx} = y \quad \text{--- (3.51)}$$

differentiating eqⁿ (3.50) w.r.t x we get

$$\frac{d^2v}{dx^2} = z \frac{dI}{dx}$$

Substituting (3.51) in above eqⁿ (1):

$$\frac{d^2v}{dx^2} = z(yv) \quad \text{--- (3.52)}$$

$$\frac{d^2v}{dx^2} = yz v \quad \text{--- (3.52)}$$

The solution of eqⁿ (3.52) this diff. eqⁿ (3.52) is

$$V = K_1 \cosh(\alpha \sqrt{yz} x) + K_2 \sinh(\alpha \sqrt{yz} x) \quad \text{--- (3.53)}$$

differentiating 3.53 wrt x we have

$$\frac{dV}{dx} = K_1 \sinh(x\sqrt{yz}) \sqrt{yz} + K_2 \cosh(x\sqrt{yz}) \sqrt{yz}$$

$$\text{But } \frac{dV}{dx} = IZ \quad (\because \text{by 3.50})$$

$$IZ = K_1 \sqrt{yz} \cdot \sinh(x\sqrt{yz}) + K_2 \sqrt{yz} \cdot \cosh(x\sqrt{yz})$$

~~$I = \sqrt{\frac{y}{z}} [K_1 \sinh(x\sqrt{yz}) + K_2 \cosh(x\sqrt{yz})]$~~

$$I = \sqrt{\frac{y}{z}} [K_1 \sinh(x\sqrt{yz}) + K_2 \cosh(x\sqrt{yz})] \quad \text{--- (3.54)}$$

eqns 3.53 and 3.54 give the expressions for V & I in the form of unknown constants K_1 and K_2 the values of K_1 and K_2 can be formed by applying end conditions as under,

$$\text{At } x=0, \quad V = V_R \quad \text{and} \quad I = I_R$$

Putting these values in eqn 3.53 we have

$$V_R = K_1 \cosh(0) + K_2 \sinh(0)$$

$$V_R = K_1 (1)$$

$$\therefore V_R = K_1$$

Similarly putting $x=0$ $V=V_R$ & $I=I_R$ in eqn 3.54

$$I_R = \sqrt{\frac{y}{z}} [K_1 \sinh(0) + K_2 \cosh(0)]$$

$$I_R = K_2 \sqrt{\frac{y}{z}}$$

$$K_2 = I_R \sqrt{\frac{z}{y}}$$

Substituting the values of K_2 and K_1 in eqn 3.53 & 3.54 we get

$$V = V_R \cosh(x\sqrt{yz}) + I_R \sqrt{\frac{z}{y}} \sinh(x\sqrt{yz})$$

The sending end vtg V_s and sending end current I_s are obtained by putting $x=l$ in the above eqns i.e taking V as V_s and I as I_s

$$V_s = V_R \cosh(l\sqrt{yz}) + I_R \sqrt{\frac{z}{y}} \sinh(l\sqrt{yz})$$

$$I_s = \sqrt{\frac{y}{z}} [V_R \sinh(l\sqrt{yz}) + I_R \sqrt{\frac{z}{y}} \cosh(l\sqrt{yz})]$$

$$\sqrt{YZ} = \sqrt{|Y| |Z|} = \sqrt{YZ}$$

$$\sqrt{\frac{Y}{Z}} = \sqrt{\frac{|Y|}{|Z|}} = \sqrt{\frac{Y}{Z}}$$

Y = total shunt admittance of line

Z = total series impedance of line.

∴ expression for V_s and I_s becomes

$$V_s = V_R \cosh \sqrt{YZ} + I_R \sqrt{\frac{Z}{Y}} \sinh \sqrt{YZ} \quad \text{--- (3.55)}$$

$$I_s = Y_R \sqrt{\frac{Y}{Z}} \sinh \sqrt{YZ} + I_R \cosh \sqrt{YZ} \quad \text{--- (3.56)}$$

~~13/17~~

It is helpful to expand hyperbolic sin and cosh in terms of their power series

$$\cosh \sqrt{YZ} = \left(1 + \frac{YZ}{2} + \frac{Y^2 Z^2}{24} + \dots \right) \quad \text{approx}$$

$$\sinh \sqrt{YZ} = \left(\sqrt{YZ} + \frac{(YZ)^{3/2}}{6} + \dots \right) \quad \text{approx}$$

3.7 A 3φ TC 200km long has following constants

Resistance per phase per km is 0.16Ω

Reactance per phase per km is 0.25Ω

Shunt admittance per phase per km is $1.5 \times 10^{-6} \text{ S}$

Calculate by rigorous method sending end vtg & sending end current when the line is delivering a load of 20MW at 0.8 pf (lag)

the receiving end vtg is kept constant at 110kV

$$L = 200 \text{ km}$$

$$P_d = 200 \text{ MW}$$

$$\text{total } R = 0.16 \times 200 = 32 \Omega$$

$$\text{total } X_L = 0.25 \times 200 = 50 \Omega$$

$$\text{total } Y = j1.5 \times 10^{-6} \times 200 = j0.0003 = 0.0003 \angle 90^\circ \text{ S}$$

$$\text{Total impedance} = Z = R + jX_L$$

$$Z = 32 + j50 \Omega$$

$$Z = 59.36 \angle 57.38^\circ$$

$$V_R(\text{line}) = 110 \text{ kV}$$

$$V_R(\text{phase}) = \frac{110 \text{ kV}}{\sqrt{3}} = 63508.53 \text{ V}$$

$$I_R = \frac{P_d}{\sqrt{3} V_R \cos \phi} = \frac{P_d}{3 V_{Rph} \cos \phi} = \frac{200 \text{ MW}}{3 \times 63508.53 \times 0.8} = 131 \text{ A}$$

$$\vec{V}_S = 67018 + j6840 \text{ V}$$

$$V_S = 67366 \angle 5.5^\circ \text{ V}$$

$$\vec{I}_S = 129.83 + j19.42 \text{ A}$$

$$I_S = 131.1 \angle 8^\circ \text{ A}$$

$$\frac{90+58}{2} = \angle 74$$

$$\sqrt{YZ} = \sqrt{0.0003 \angle 90 \times 59.36 \angle 57.38} = \sqrt{0.0178 \angle 147.38} = 0.133 \angle 74$$

$$YZ = 0.0178 \angle 147.38$$

$$Y^2 Z^2 = (0.0003 \angle 90)^2 (59.36 \angle 57.38)^2 = 0.00032 \angle 296$$

$$\sqrt{\frac{Z}{Y}} = \frac{445}{0.0003 \angle 90} \sqrt{59.36 \angle 57.38} = 445 \angle -82 \angle \frac{58-90}{2} = \angle -16$$

$$\sqrt{\frac{Y}{Z}} = \sqrt{\frac{0.0003}{59.36} \angle \frac{90-58}{2}} = 0.0024 \angle 16$$

$$\cosh \sqrt{YZ} = \left(1 + \frac{YZ}{2} + \frac{Y^2 Z^2}{24} + \dots \right)$$

$$\cosh \sqrt{YZ} = \left(1 + \frac{0.0178 \angle 147.38}{2} + \frac{0.00032 \angle 296}{24} \right) = 0.992 \angle 0.2762$$

$$\sinh \sqrt{YZ} = \left(\sqrt{YZ} + \frac{(YZ)^{3/2}}{6} + \dots \right)$$

$$= \left(0.133 \angle 74 + \frac{(0.0178 \angle 147.38)^{1/2}}{6} \right)^3$$

$$= 0.1325 \angle 74.6$$

Jun 14

Ferromagnetic effect on transmission line

* Generalised circuit constants of a transmission line

In any four terminal network; The input voltage (V_s) & input current (I_s) can be expressed in terms of o/p vtg (V_R) & o/p current (I_R) incidently a transmission line is a four terminal network.:

Two input terminals where power enters the n/w and two o/p terminals where power leaves the n/w

The input voltage \vec{V}_s and input current \vec{I}_s of a 3p TL can be expressed as

$$\vec{V}_s = \vec{A} \vec{V}_R + \vec{B} \vec{I}_R \quad \text{--- 3.57}$$

$$\vec{I}_s = \vec{C} \vec{V}_R + \vec{D} \vec{I}_R \quad \text{--- 3.58}$$

Where $\vec{V}_s =$ Sending end voltage / ph

$\vec{I}_s =$ current / ph

$\vec{I}_R =$ Receiving end current / ph

$\vec{V}_R =$ vtg / ph

And $\vec{A}, \vec{B}, \vec{C}$ & \vec{D} (Generally complex numbers are the constant known as generalised ckt constant of the TL. The value of constant depends upon the particular method adopted for solving TL. Once the values of these constants are known, performance calculation of the line can be easily

Determination of Generalised constants of T.L

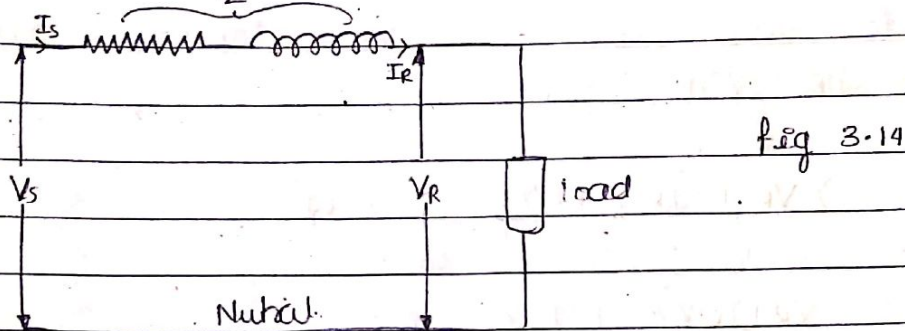
As stated previously the send end voltage (\bar{V}_s) and sending end C/n \bar{I}_s of the TL can be expressed as

$$\bar{V}_s = \bar{A}\bar{V}_R + \bar{B}\bar{I}_R \quad \text{--- (3.59)}$$

$$\bar{I}_s = \bar{C}\bar{V}_R + \bar{D}\bar{I}_R \quad \text{--- (3.60)}$$

We shall now determine the values of constants for diff Transmission lines

(i) Short Transmission Line



In the short TL the effect of line capacitance is neglected there for the line is considered to have series impedance.

Fig 3.14 above shows 3 ϕ TL on single ϕ bases

$$\bar{I}_s = \bar{I}_R \quad \text{--- (3.61) and}$$

$$\bar{V}_s = \bar{V}_R + \bar{I}_R \bar{Z} \quad \text{--- (3.62)}$$

Comparing eqⁿ 3.59 and 3.60 we have

$$\bar{A} = 1; \quad \bar{B} = \bar{Z}; \quad \bar{C} = 0 \quad \text{and} \quad \bar{D} = 1$$

Identically $\bar{A} = \bar{D}$

$$\text{and} \quad \bar{A}\bar{D} - \bar{B}\bar{C} = 1 \times 1 - \bar{Z} \times 0 = 1$$

(iii) Medium Transmission Line. (Nominal 'T')

In this method the whole line to neutral capacitance is assumed to be connected at the middle point of the line and either side shown fig - 3.15

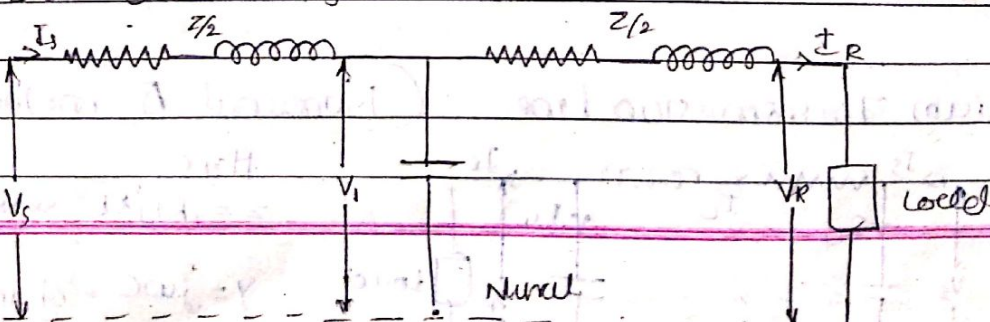


Fig 3.15

Here $\bar{V}_s = \bar{V}_1 + \bar{I}_s \bar{z}/2$ — (3.63)

$\bar{V}_1 = \bar{V}_R + \bar{I}_R \bar{z}/2$ — (3.64)

$\bar{I}_c = \bar{I}_s - \bar{I}_R$ — (3.65)

$\bar{I}_c = \bar{V}_1 \bar{Y}$

where $Y =$ shunt admittance.

$\bar{I}_c = \bar{Y} \left(\frac{\bar{V}_R + \bar{I}_R \bar{z}}{2} \right)$ — (3.66)

$\therefore \bar{I}_s = \bar{I}_R + \bar{Y} \left(\frac{\bar{V}_R + \bar{I}_R \bar{z}}{2} \right)$

$\bar{I}_s = \bar{I}_R + Y \bar{V}_R + \frac{Y \bar{I}_R \bar{z}}{2}$

$\bar{I}_s = Y \bar{V}_R + \bar{I}_R \left(1 + \frac{Y \bar{z}}{2} \right)$ — (3.67)

and $\bar{V}_s = \bar{V}_R + \bar{I}_R \bar{z}/2 + \bar{I}_s \bar{z}$

$\bar{V}_s = \left(1 + \frac{Y \bar{z}}{2} \right) \bar{V}_R + \left(\frac{\bar{z}}{2} + \frac{Y \bar{z}^2}{2} \right) \bar{I}_R$ — (3.68)

Comparing 3.59 with 3.68 and 3.60 with 3.67 we have

$A = \left(1 + \frac{Y \bar{z}}{2} \right)$, $B = \left(\frac{\bar{z}}{2} + \frac{Y \bar{z}^2}{2} \right) = \bar{z} \left(1 + \frac{Y \bar{z}}{2} \right)$

$C = Y$, $D = \left(1 + \frac{Y \bar{z}}{2} \right)$

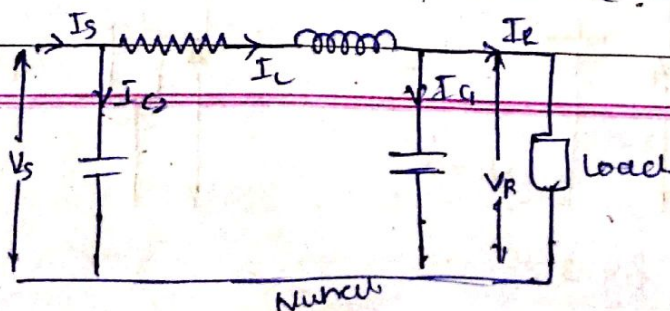
$\therefore A = D$

and $AD - BC = \left(1 + \frac{Y \bar{z}}{2} \right)^2 - \frac{Y \bar{z}}{2} \left(1 + \frac{Y \bar{z}}{2} \right)$

$= 1 + \frac{Y^2 \bar{z}^2}{4} + \frac{Y \bar{z}}{2} - \frac{Y \bar{z}}{2} - \frac{Y^2 \bar{z}^2}{4}$

$AD - BC = 1$

Medium Transmission line (Nominal π method)



Here.

$Z = R + jX_L$ series impedance

$Y = jW_C =$ shunt admittance

$I_s = I_c + I_R$

$$\bar{I}_S = \bar{I}_L + \bar{I}_C$$

$$\bar{I}_S = \bar{I}_L + \bar{V}_S \cdot \bar{Y}/2$$

$$\bar{I}_L = \bar{I}_R + \bar{I}_C$$

$$\bar{I}_L = \bar{I}_R + \bar{V}_R \bar{Y}/2$$

$$\therefore \bar{V}_S = \bar{V}_R + \bar{I}_L \bar{Z} = \bar{V}_R + (\bar{I}_R + \bar{V}_R \bar{Y}/2) \bar{Z} \quad \text{Putting } \bar{I}_L$$

$$\bar{V}_S = \bar{V}_R \left(1 + \frac{\bar{Y}\bar{Z}}{2}\right) + \bar{I}_R \bar{Z}$$

$$\bar{I}_S = \bar{I}_L + \bar{V}_S \bar{Y}/2$$

$$\bar{I}_S = (\bar{I}_R + \bar{V}_R \bar{Y}/2) + \bar{V}_S \bar{Y}/2 \quad (\because \text{putting } \bar{I}_L)$$

Putting value of \bar{V}_S

$$\bar{I}_S = \bar{I}_R + \bar{V}_R \frac{\bar{Y}}{2} + \frac{\bar{Y}}{2} \left\{ \bar{V}_R \left(1 + \frac{\bar{Y}\bar{Z}}{2}\right) + \bar{I}_R \bar{Z} \right\}$$

$$= \bar{I}_R + \bar{V}_R \frac{\bar{Y}}{2} + \bar{V}_R \frac{\bar{Y}}{2} + \bar{V}_R \frac{\bar{Y}^2 \bar{Z}}{4} + \bar{Y} \bar{I}_R \bar{Z}$$

$$\bar{I}_S = \left(1 + \frac{\bar{Y}\bar{Z}}{2}\right) \bar{I}_R + \bar{Y} \left(1 + \frac{\bar{Y}\bar{Z}}{4}\right) \bar{V}_R$$

$$\bar{A} = \bar{D} = \frac{1 + \bar{Y}\bar{Z}}{2} \quad \bar{C} = \bar{Y} \left(1 + \frac{\bar{Y}\bar{Z}}{4}\right) \quad \left. \begin{array}{l} \\ \end{array} \right\} \begin{array}{l} \\ \end{array} \text{Compensating}$$

$$\bar{B} = \bar{Z}$$

Long Transmission Lines

$$\bar{V}_S = \bar{V}_R \cosh \sqrt{\bar{Y}\bar{Z}} + \bar{I}_R \sqrt{\frac{\bar{Z}}{\bar{Y}}} \sinh \sqrt{\bar{Y}\bar{Z}}$$

$$\bar{I}_S = \bar{V}_R \sqrt{\frac{\bar{Y}}{\bar{Z}}} \sinh \sqrt{\bar{Y}\bar{Z}} + \bar{I}_R \cosh \sqrt{\bar{Y}\bar{Z}}$$

$$\bar{V}_S = \bar{A} \bar{V}_R + \bar{B} \bar{I}_R$$

$$\bar{I}_S = \bar{C} \bar{V}_R + \bar{D} \bar{I}_R$$

$$\bar{A} = \bar{D} = \cosh \sqrt{\bar{Y}\bar{Z}}$$

$$\bar{B} = \sqrt{\frac{\bar{Z}}{\bar{Y}}} \sinh \sqrt{\bar{Y}\bar{Z}}$$

$$\bar{C} = \sqrt{\frac{\bar{Y}}{\bar{Z}}} \sinh \sqrt{\bar{Y}\bar{Z}}$$

Mod-1
Electrical Power Sys. by Ashfaq Hussain
Conductor copper, etc
5-10-3

1) A 132 kV 50 Hz 3 ϕ TL delivers a load of 50 MW at 0.8 PF lag at the receiving end the generalised constants of 3 ϕ TL are $A=D=0.95 \angle 1.4^\circ$, $B=96 \angle 78^\circ$, $C=0.0015 \angle 90^\circ$. Find the regⁿ of the line and charging % Use nominal T

Given

$$V_R(\text{line}) = 132 \text{ kV}$$

$$V_A(\text{ph}) = 76210.23$$

$$I_R = \frac{P_R}{\sqrt{3} V_R \cos \phi} = \frac{50 \text{ M}}{\sqrt{3} \cdot 132 \text{ k} \cdot 0.8} = \frac{50 \text{ M}}{3 \times 76210.23 \times 0.8} = 273.3$$

$$\cos \phi_R = 0.8$$

$$\sin \phi_R = 0.6$$

Taking receiving end v_{tg} at reference phasor

$$\vec{V}_R = V_R + j0 =$$

$$\vec{I}_R = I_R (\cos \phi_R - j \sin \phi_R) = I_R \angle -\phi_R = 273.3 \angle -36.86$$

Sending end voltage

$$\vec{V}_S = A \vec{V}_R + B \vec{I}_R$$

$$= (0.95 \angle 1.4^\circ \times 76210.23 \angle 0^\circ) + (96 \angle 78^\circ \times 273.3 \angle -36.86)$$

$$\vec{V}_S = 94.056 \text{ k} \angle 11.66 \text{ kV}$$

$$\vec{I}_S = (0.0015 \angle 90^\circ) (76.21 \text{ k}) + (0.95 \angle 1.4^\circ) \cdot (273.3 \angle -36.86)$$

$$\vec{I}_S = 214.315 \angle -9.71$$

$$\% R = \frac{V_S - V_R}{V_R} \times 100 = \frac{94.056 \text{ k} - 76.21 \text{ k}}{76.21 \text{ k}} \times 100 = 23.41$$

$$\vec{I}_C = \vec{I}_S - \vec{I}_R$$

$$= 128.2 \angle 93.1 \text{ A}$$

$$\% R = \frac{V_S - V_R}{V_R} \times 100 = 23.41$$

$$V_S = A \vec{V}_R + B \vec{I}_R$$

as at no load $\vec{I}_R = 0$

$$\therefore V_S = A \vec{V}_R$$

$$\therefore \% R = \left(\frac{V_S}{A} - V_R \right) / V_R \times 100$$